A Library of High Level Control Operators *

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Abstract

Numerous high-level control operators, with various properties, exist in the literature. To understand or compare them is difficult since their definitions use quite different theoretical frameworks; moreover, to our knowledge, no implementation offers them all. This paper tries to explain control operators by the often simple stack manipulation they perform. We therefore present what we think these operators are, in an executable framework derived from abstract continuations. This library is published in the hope that it will be useful, but WITHOUT ANY WARRANTY; without even the implied warranty of MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. For instance, we do not claim our implementation to be faithful nor we attempt to formally derive these implementations from their original definitions. The goal is to give a flavor of what control operators are, from an implementation point of view. Last but worth to say, all errors are mine.

Among the many existing control operators, we only consider call/cc, prompt/control, shift/reset, sequential spawn, splitter/abort/call/pc. We also add dynamic-wind to them although it does not belong to the same family of control operators.

Our lingua franca is Scheme extended with a simple class definition facility. We use Scheme (i) to avoid frightening Greek letters and, (ii) to provide implementations people can play with in any plain Scheme system. Our defining process is two-fold: first, we use a program transformation making continuations apparent: Abstract Continuation Passing Style (ACPS) [FWFD88]. ACPS is somewhat similar to Continuation Passing Style (CPS) but confers a richer structure to continuations. ACPS represents continuations by lists of "continuation slices". Implementors will recognize in these slices a functional abstraction for stack frames. In a second step, the rewritten equivalent program is evaluated with any regular Scheme evaluator. The key point is the use of ACPS which allows control operators to be written as regular (but reflective) Scheme functions acting on the representation of continuations. Our presentation has the definite advantage to be executable and to offer all these control operators altogether.

The paper has the following structure: we first present ACPS then exercise it on the well-known call/cc operator. This will be followed by a brief description of what partial continuations are. We will then expose the various sets of control operators¹.

1 Abstract Continuation Passing Style

CPS is a program transformation that makes continuations apparent. CPS also corresponds to a programming style where functions take an additional argument, the continuation: an unary function which is applied to the value that would have been returned in normal style. Continuations come from the work of Strachey and Wadsworth [SW74, Rey93] and were used to denote control features such as goto i.e., unconditional jump. CPS and sophisticated control handling have always been sources of inspiration, see [DL92, SF92, Mor92, FSDF93, Sit93] for recent developments.

Denotational techniques often drift into program transformations: CPS was exploited in Rabbit, the first Scheme compiler [Ste78], as a kind of intermediate language. CPS provides a simple (but not unique)

^{*}Id: contlib.bk,v 1.26 1994/02/04 19:41:34 queinnec Exp . Submitted to Lisp Pointers.

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¹Their definition is the actual code as it appears in the contlib.tar.gz package and automatically extracted using LiSP2TEX. See the Scheme Repository or ftp.inria.fr:IMRIA/Projects/icsla/Programs to get them.

mean to compile programs using call/cc: CPS turns these programs into new equivalent programs where continuations are represented by regular closures which only require normal compiling technology². In other terms, CPS turns call/cc into a regular function that the user could have directly written³:

```
(define (CPS-call/cc k1 f)
```

(f k1 (lambda (k2 value) (k1 value))))

In this definition, continuations appear as the first variable (this makes easier the introduction of dotted variables) with a name conventionally prefixed by k: functional applications therefore take the current continuation as first argument. Being a function, the reified continuation obeys the CPS protocol: it takes a continuation as first argument (k2) then forgets it and, finally applies k1 to value. CPS-style continuations are closures i.e., opaque objects that can only be applied. More elaborate control operators need more information about the continuation.

Abstract continuations were introduced in [FWFD88] to describe the meaning of prompt and control operators. We use its syntactic counterpart and encode continuations as lists of frames. With an implementation bias, a frame will be represented by an object whose first slot contains a behavior i.e., a binary function that expects a stack (composed of all the frames that are below this very frame) and a value. When a frame is activated, it computes a new value to be sent back to the rest of the frames. Frames are represented by objects and not directly by behaviors so that they can be recognized and specialized to hold extra slots (other than behaviors), this will be needed later by some control operators.

Since the continuation is no longer represented by a function, we ought to provide the necessary procedures that encapsulate its representation: a value is sent to a continuation using **resume**. A frame is added, i.e., pushed, onto a continuation using **extend**.

```
(define-class frame Object (behavior))
(define (resume q v)
  ((frame-behavior (car q)) (cdr q) v) )
(define (extend q frame)
  (cons frame q) )
```

The define-class form defines a new class known as frame (subclass of the root class here named Object). A frame has a single slot that contains its behavior. This behavior can be extracted from a frame using the frame-behavior selector; make-frame builds a new frame out of a behavior; finally, a frame can be recognized with the frame? predicate. We use objects rather than records since we use inheritance in the resume function: the frame-behavior selector will thus work for any direct or indirect instances of frame⁴.

As shown in the definition of **resume**, a behavior is a binary function taking a continuation and a value. A continuation is represented by a list of frames. To send a value to a continuation corresponds to the application of the behavior of the first frame to the rest of the frames and to the received value. This tightly mimics the behavior of a frame that receives a value and has access to the frames that are below it.

The ACPS program transformation appears in table 1, see [Que92b] for a variant. Computations are split into small atomic computation steps. A computation step is fed with a value and a continuation, may extend the continuation with new computations to be done or just gives a value back to the continuation. Making frames apparent allows some compile-time analyzes to compact the continuation or to remove some kinds of associatively wrapped recursions [Que93].

ACPS-transformed programs contain a lot of administrative redexes: elaborate algorithms [DF92, SF92] can be devised to avoid their generation. One can also observe that CPS may be recovered from ACPS with a special encoding of **resume** and **extend**:

```
(define (resume q v) (q v))
(define (extend q frame)
  (lambda (v) ((frame-behavior frame) q v)) )
```

To project an ACPS-transformed program into a CPS-transformed program i.e., to transform inspectable lists of frames into opaque closures, restrict the possibility of introspection which is the basis of reflective programming [dRS, FW84, Wan86, dR87, WF88, DM88].

²To compile well these closures requires a higher compiling technology [App92].

³This is true only if the user can submit such a definition and prevent the evaluator to CPS-convert it.

⁴We use our own home-made object system called MEROONV3, consult again the Scheme repository to get it.

```
\begin{aligned} & A C \mathcal{PS}[\![\nu]\!]q = (\text{resume } q \ \nu) \text{ if } \nu \text{ is a non global variable} \\ & A C \mathcal{PS}[\![\nu]\!]q = (\text{resume } q \ A C P S - \nu) \text{ if } \nu \text{ is a global variable} \\ & A C \mathcal{PS}[\![(\text{quote } \varepsilon)]\!]q = (\text{resume } q \ (\text{quote } \varepsilon)) \\ & A C \mathcal{PS}[\![(\text{if } \pi_0 \ \pi_1 \ \pi_2)]\!]q = A C \mathcal{PS}[\![\pi_0]\!](\text{extend } q \ (\text{make-frame } (\lambda(q' \ v') \ (\text{if } v' \ A C \mathcal{PS}[\![\pi_1]\!]q' \ A C \mathcal{PS}[\![\pi_2]\!]q')))) \\ & A C \mathcal{PS}[\![(\text{set! } \nu \ \pi)]\!]q = A C \mathcal{PS}[\![\pi]\!](\text{extend } q \ (\text{make-frame } (\lambda(q' \ v') \ (\text{resume } q' \ (\text{set! } \nu \ v'))))) \\ & A C \mathcal{PS}[\![(\lambda(v^*) \ \pi)]\!]q = (\text{resume } q \ (\lambda(q' \ v^*) \ A C \mathcal{PS}[\![\pi]\!]q')) \\ & A C \mathcal{PS}[\![(\pi_1 \ \dots \ \pi_n)]\!]q_0 = \\ & A C \mathcal{PS}[\![\pi_1]\!](\text{extend } q_0 \ (\text{make-frame } (\lambda(q_1 \ v_1) \ \dots \ A C \mathcal{PS}[\![\pi_n]\!](\text{extend } q_{n-1} \ (\text{make-frame } (\lambda(q_n \ v_n) \ (v_1 \ q_n \ v_2 \ \dots v_n))))...))) \\ & \text{Table 1: A C PS rules} \end{aligned}
```

To end this section, we give the usual factorial function as transformed by ACPS and massaged a little to avoid administrative redexes.

An interesting point of this massaged form is related to errors like trying to multiply a non-number. If the error handling system allows you to correct this on the fly, then obviously the multiplication has a mean to reify and use (infra-)continuations that do not appear in the above program.

The continuation of the internal recursive call to ACPS-fact explicitly shows the pending multiplication frame, [Que93] takes benefit of this static observation to combine frames together thus opening new opportunities for optimizations. ACPS is very expressive and can be used to describe implementations of dynamic variables, error handling, multitasking [Que92b, Que92a, QD93].

2 À tout seigneur, tout honneur: call/cc

The call/cc operator is the basic control operator of Scheme. It reifies the current continuation into a function and applies its sole argument on it, the value of this application becomes the value of the original call/cc form. call/cc can be used to program any sequential control operator and, at least, multitasking [Wan80], engines [HF84], escapes [HFW84] and even partial continuations! From a more implementational point of view, three usages can be recognized:

- escape operator: the continuation is only invoked once and only while in the dynamic extent of the call/cc form that created it. This usage provides a setjmp/longjmp facility à la C, catch/throw and variants à la COMMON LISP, call/ep à la PaiLisp [IM89] etc.
- coroutine operator: the computation is reified into a continuation, which will be invoked at most once later. An example of coroutine scheduler appear in [Wan80, Mat92];
- the last case is when a continuation is multiply invoked i.e., multiple values are returned to the same continuation. This can be used by generators à la Icon [MH90] but also appears in presence of concurrency [QD93].

The definition of call/cc as defined in [CR91] and according to ACPS, is as simple as it was according to CPS. Observe the duplication of q1 which is still the current continuation of the call to f as well as a part of the reified continuation. This apparent simplicity must not hide the fact that continuations are difficult to compile and implement efficiently as can be seen in [CHO88, HD90, JG89, Mat92].

```
(define (ACPS-call/cc q1 f)
  (f q1 (lambda (q2 value) (resume q1 value))) )
```

Figure 1: call/cc

3 Partial continuations

Consider the following function, which uses call/cc to perform a premature exit. It receives a list of numbers to multiply:

Whenever a zero is found, an immediate escape is performed to directly return zero without performing any multiplications. Suppose we invoke multiply-list on $(4 \ 3 \ 2 \ 0 \ \ldots)$, to escape means that, when zero is encountered, a prefix of the continuation (the prefix that is waiting for a value to multiply by 2, 3 and 4) will suddenly disappear. Rather than just erasing this prefix from the stack, one might imagine to turn it into an interesting programmatic object: this is the essence of partial continuations. Still using the previous example, the partial continuation represents three pending multiplications and is equivalent to $\lambda x.4 * (3 * (2 * x))$.

Once reified, a partial continuation can be used as a regular function. Unlike continuations, partial continuations return a value and therefore can be composed. A partial continuation is a "continuation slice" which may be viewed as the "difference" of two regular continuations [MQ93]. A partial continuation is thus identified by two points in a stack and all partial continuation control operators offer the three following functionalities:

- 1. to identify where a partial continuation starts,
- 2. to identify where a partial continuation finishes,
- 3. to reify a partial continuation between these two points.

Very often, the two last actions are not separated, they are performed in one go.

Partial continuations appeared in [FFDM87, FFDM87, FF87] as well as in [Joh87, JD88]. Many papers follow in the Scheme realm and among them [Fel88, DF90, HD90, QS91, MQ93]. A detailed example of partial continuation use appears in [Dan89].

4 Useful functions

We introduce some functions to ease the forthcoming definitions. extend* takes a list of frames whereas extend takes only one frame. The split operator takes a continuation q, a predicate, a success function and a failure thunk. It looks for the first tail of q that satisfies the predicate. If such a tail is found then the success function is called on this tail as well as on the list of frames that precede the found tail; otherwise, the failure thunk is invoked.

```
(define (extend* q frames)
 (if (pair? frames)
    (extend (extend* q (cdr frames)) (car frames))
    q ) )
(define (split q predicate success failure)
 (define (scan q frames)
    (if (pair? q)
        (if (predicate q)
            (success (reverse frames) q)
            (scan (cdr q) (cons (car q) frames)) )
        (failure) ) )
    (scan q '()) )
```

The control operators are generally programmed as follow: the beginning of a partial continuation is identified by a special frame pushed onto the stack. When a partial continuation needs to be reified, the **split** function is used on the current continuation to find the frames that are above this special frame. These frames, properly wrapped with a functional interface, represent the partial continuation.

The definitions below do not take efficiency into account but they try to suggest that there exist common patterns.

5 prompt, control

Two control operators, prompt and control, were presented and discussed in [Fel88, FWFD88, SF90a, SF90b]. The prompt operator identifies contexts to be used by control. The control function reifies the context up to the nearest dynamically enclosing prompt, into a partial continuation and, at the same time, removes it from the current continuation. prompt is a syntax which expands into a call to prompt-evaluate; remember that prompt-evaluate is ACPS-transformed into ACPS-prompt-evaluate.

To define these control operators, we use a subclass of frame: prompt-frame, to mark the presence of a prompt; its behavior is similar to the identity, as represented by resume: it just passes the value it receives back to the stack below it. prompt-evaluate pushes a prompt-frame onto the stack and then invokes its first argument: a thunk. When invoked, control unwinds the frames of the current continuation until finding a prompt-frame, wraps all unwound frames into a regular function and applies its argument on it.

5.1 Examples

Here are some simple examples of prompt/control that illustrate various points. More comprehensive examples are given in the above references.

(prompt (* 2 (control (lambda (f) 3))))	<u>→</u> 3	[a]
(prompt (* 2 (control (lambda (f) (* 5 (f 3))))))	→ 30	[b]
(prompt (* 2 (control (lambda (f) (f (f 3))))))	\rightarrow 12	[c]
((prompt (* 2 (control (lambda (f) f)))) 3)	$\rightarrow 6$	[d]

In these four examples, the partial continuation is $\lambda x.2*x$. When **control** reifies this partial continuation, it removes its associated frames from the stack as shown in example [a]. This is an "abort", an imperative effect. The partial continuation is a regular function that yields a value, as shown in [b]; hence partial continuations are composable, see example [c]. Once reified, there is no restriction on the use of partial continuations: they can be used out of the extent of the control form that creates them as illustrated on example [d].

These examples are simple and show the interest of partial continuations. Unfortunately, there are more complex usages when control operators are called from within the reified continuation. It is difficult to figure out what is natural in these cases and we will see that it is a divergence point between the various sets of control operators.

```
(prompt (* 5
                                                                                                    [e]
             (prompt (* 2
                           (control (lambda (f2)
                                                                         ; f2= \lambda x.2 * x
                                        (* 3 (control (lambda (f3) ;f3=\lambda x.3 * x
                                                           7 ))) )) )) \rightarrow 35
                                                                                                    [f]
(prompt (* 5 (
                 (prompt (* 2
                              (control (lambda (f2)
                                                                               ; f2= \lambda x.2 * x
                                            (lambda ()
                                              (* 3 (control (lambda (f3) ;f3=\lambda x.5*(3*x)
                                                                 7 ))) ) )) ))) )))
                                                              → 7
(prompt (* 5
                                                                                                    [g]
              ((lambda (x)
                                                 ; let \phi be this abstraction
                 (control (lambda (f1)
                                                 ;f1= \lambda v.2 * 5 * v
                              x)))
               (* 3 (control (lambda (f2) ;f2= \lambda u.5 * \phi(3 * u)
                                  (* 2 (f2 7))))))) \rightarrow 21
```

Example [e] exhibits the effect of a control inside a control, the two control forms reify a partial continuation up to the same prompt. On the contrary, example [f] shows embedded control forms reiying up to different prompt forms. The final example [g] shows control called from inside the application of a reified partial continuation. These examples are complex and require some care to be checked.

5.2 call/cc with prompt/control

The control operator is somewhat dynamic since it looks for the nearest enclosing prompt-frame in the continuation. This dynamic behavior of control poses problems of capture similar to those posed by dynamic variables in traditional Lisp interpreters. To arbitrarily wrap an expression into a prompt form i.e., to replace π by (prompt π) may thus have a non-local effect. Using multiple embedded control forms is difficult but can be done if some protocol is added around each prompt form as studied in [SF90a].

The call/cc operator can be defined with these operators. Given a program π not using prompt, we can provide the call/cc facility, rewriting π as:

```
(let ()
  (define (call/cc f)
```

```
(prompt \pi))
```

Reciprocally, prompt and control can be simulated with call/cc (and assignment) as explained in [SF90a].

6 shift/reset

Danvy and Filinski introduced in [DF90, DF89] a new couple of control operators: reset and shift; reset identifies the contexts up to which shift reifies partial continuations. A shift form reifies its context up to the dynamically nearest reset form and removes it from the current continuation. reset and shift are syntaxes that we expand into functions taking thunks as argument: reset-evaluate and shift-evaluate.

One interesting difference with prompt/control lies in the definition of the reified partial continuation: it now contains (and finishes with) the nearest reset-frame. Therefore partial continuations have at least their invocation point as enclosing context.

```
(define-class reset-frame frame ())
(define-syntax reset
  (syntax-rules ()
    ((_ expression) (reset-evaluate (lambda () expression))) ) )
(define-syntax shift
  (syntax-rules ()
    ((_ variable expression)
     (shift-evaluate (lambda (variable) expression)) ) ) )
(define (ACPS-reset-evaluate q thunk)
  (thunk (extend q (make-reset-frame resume))) )
(define (ACPS-shift-evaluate q f)
  (split q (lambda (q) (reset-frame? (car q)))
         (lambda (frames q)
           (let ((frames (append frames (list (car q)))))
             (f q (lambda (q v)
                    (resume (extend* q frames) v) )) ))
         (lambda () (error "No enclosing reset")) ) )
                              Figure 3: reset/shift
```

6.1 Examples

Here are the previous examples rewritten with these new control operators. Examples were similarly named to ease comparison. There are no divergence in the six first examples, from [a] to [f].

(reset (* 2 (shift f 3))) $\rightarrow 3$ [a] (reset (* 2 (shift f (* 5 (f 3)))) \rightarrow 30 [b] (reset (* 2 (shift f (f (f 3))))) [c] \rightarrow 12 ((reset (* 2 (shift f f))) 3) $\rightarrow 6$ [d] (reset (* 5 [e] (reset (* 2 (shift f2 ; $f2 = \lambda x \cdot reset(2 * x)$ (* 3 (shift f3 ;f3= $\lambda x.reset(3 * x)$ 7)))))))) → 35 (reset (* 5 ([f]

```
(reset (* 2) (shift f2) ; f2 = \lambda x.reset(2 * x) (lambda ()) (* 3 (shift f3); f3 = \lambda x.reset(5 * 3 * x) 7))))) \rightarrow 7
(reset (* 5) [g] ((lambda (x)) ; let \phi be this abstraction (shift f1 x)) ; f1 = \lambda v.reset(5 * v) (* 3 (shift f2) ; f2 = \lambda u.reset(5 * \phi(3 * u))) (* 2 (f2 7)))) \rightarrow 42
```

A difference can be observed in the seventh example [g]. The reason is that when the partial continuation f2 is invoked, the (shift f1 x) form reifies up to the nearest reset-frame and thus do not capture the pending multiplication by 2 since the call to f2 reinstalls a reset-frame.

6.2 call/cc with shift/reset

As for the other control operators, it is possible to program call/cc with shift and reset. Once again, the program π is required not to use reset to avoid interference with the coding of call/cc. The program π is wrapped as:

7 spawn

Hieb and Dybvig presented, in [HD90], a new control operator called **spawn**. Although specified in presence of concurrency, **spawn** is useful even in the absence of multiple processes. We will only present a sequential version here. One of the goals of the authors was to replace the dynamic behavior of the two previous proposals by more control on the point up to which a partial continuation is reified. A consequence is that **spawn** reifies a *process controller* that can only be used while in the dynamic extent of the **spawn** form that created it. The reason is that if you want to reify up to a **spawn** point, this point must exist somewhere in your future i.e., you must be in the dynamic extent of this very **spawn** form. This problem does not exist with **control** and **shift** since they do not target a specific point but just the nearest one, whatever it is. Finally, the authors devised a functional protocol with a single special function, **spawn**, to offer the identification of the context up to which reification is needed and the identification of the reification point.

spawn takes a single argument, a unary function that will be invoked by spawn on a synthesized object named a process controller, say c. The process controller c can only be applied while in the dynamic extent of the original spawn form. Whenever applied, it takes a single argument: an unary function that it applies on the reified partial continuation that extends up to the associated spawn; at the same time the process controller removes this partial continuation from the current continuation. Similarly to shift, the reified partial continuation retains the spawn-frame up to which it is reified. spawn can be viewed as a generalized prompt creating a new control function at each invocation.

7.1 Examples

To give a flavor of spawn, let us once again rewrite the former examples. With respect to the previous section and roughly said, reset is changed into (spawn (lambda (c) ...)) while (shift f ...) is replaced by (c(lambda (f) ...)). This works well if there is a single reset form but if there are more, then we can choose up to which one reification is wanted, see for instance, examples [f1] and [f2].

```
(spawn (lambda (c) (* 2 (c (lambda (f) 3))))) \rightarrow 3 \qquad [a]
```

```
Figure 4: spawn
```

```
(spawn (lambda (c) (* 2 (c (lambda (f) (* 5 (f 3)))))) \rightarrow 30
                                                                                               [b]
(spawn (lambda (c) (* 2 (c (lambda (f) (f (f 3))))))
                                                                  \rightarrow 12
                                                                                               [c]
                                                                  \rightarrow 6
                                                                                               [d]
((spawn (lambda (c) (* 2 (c (lambda (f) f)))) 3))
                                                                                               [e]
(spawn (lambda (c1)
          (* 5 (spawn (lambda (c2)
                          (* 2 (c2 (lambda (f2)
                                                                 ;f2= \lambda x.2 * x
                                       (* 3 (c2 (lambda (f3) ;f3=\lambda x.3 * x
                                                    7 ))) ))) ))) \rightarrow 35
                                                                                              [f1]
(spawn (lambda (c1)
          (* 5 ((spawn (lambda (c2)
                            (* 2 (c2 (lambda (f2)
                                         (lambda ()
                                           (* 3 (c1 (lambda (f3)
                                                       7 ))) )))))))))) \rightarrow 7
                                                                                              [f2]
(spawn (lambda (c1)
          (* 5 ((spawn (lambda (c2)
                            (* 2 (c2 (lambda (f2)
                                         (lambda ()
                                           (* 3 (c2 (lambda (f3)
                                                        7 ))) ) ))) ))) )))
  \rightarrow Out of extent error, c2 is not used in its correct dynamic extent
(spawn (lambda (c)
                                                                                               [g]
          (* 5 ((lambda (x) (c (lambda (f1) x)))
                 (* 3 (c (lambda (f2) (* 2 (f2 7))))))))))
                                                                         \rightarrow 42
((spawn (lambda (c1)
                                                                                               [h]
           (* 5 (spawn (lambda (c2)
                            (* 2 ((c1 (lambda (f1) ; f1 = \lambda u.(5 * 2 * (u))(\phi)
                                          (lambda (g) (g f1 c2)) )))) ))) ))
 ;; let \phi be the value of the following term. It will be bound to g.
 (lambda (f1 c2) (f1 (lambda () (* 7 (c2 (lambda (f2) ; f2 = \lambda v.2 * 7 * v
                                                  (* 11 (f2 13)) ))))))))
          \rightarrow 10010 i.e., 5*11*2*7*13
```

Example [g] still yields the same value; although there are two spawn-frames associated to c in the stack, spawn chooses to reify a partial continuation up to the closest. Therefore it does not capture the pending multiplication by two.

The final example is the most mind-boggling, it shows a fine example where the concept of dynamic extent appears not so intuitive. In example [h], a partial continuation f1 and a process controller c2 are used far from their birth site. f1 reinstalls the spawn-frame associated to c2 that it captured when created. Consequently, to call c2 within f1, is correct since we are still in its dynamic extent. We will return to the concept of dynamic extent in section 8.2.

7.2 call/cc with spawn

Similarly to the previous operators it is possible to write call/cc with spawn. This is even easier since now there is no restriction on programs which can use spawn for themselves without interference. The reason is that now call/cc captures the correct process controller:

8 splitter/abort/call/pc

Another set of control operators was proposed by Queinnec and Serpette in [QS91]⁵. Their effect is very close to spawn although one goal was to separate the different effects involved by spawn into different operators. splitter marks a context up to which partial continuations can be reified. The context is reified into an object called a mark which can serve as first argument to the abort, call/pc and within-extent? functions. abort allows to replace the current computation up to a given mark with a new computation expressed with a thunk. call/pc reifies the partial continuation up to the given mark and applies its second argument on it. In contrast to the previous control, shift or process controller, call/pc only reifies the partial continuation but does not remove it: this is the job of abort which is then the only imperative control operator. Similarly to spawn, marks can only be used while in the dynamic extent of the splitter form that created them and this can be tested with the within-extent? predicate adding some reflective capability to the language. Finally and similarly to control, a reified continuation does not capture the splitter-frame up to which it was reified.

8.1 Examples

Since splitter provides more basic operators, our preferred examples become more verbose. Compared to the previous section and again roughly stated, (spawn (lambda $(c) \ldots$)) is rewritten as (splitter (lambda $(c) \ldots$)) while $(c \text{ (lambda (f) } \ldots))$ is replaced by (call/pc $c \text{ (lambda (f) (abort <math>c \text{ (lambda ()} \ldots)))})$ to combine the reification and imperative abortion effect of process controller.

```
(splitter (lambda (m) (* 2 (call/pc m (lambda (f)
                                                                                            [c]
                                             (abort m (lambda ()
                                                         (f (f 3)) ))))) \rightarrow 12
(splitter (lambda (m) (* 2 (call/pc m (lambda (f) (f (f 3)))))) \rightarrow 24
                                                                                           [c1]
((splitter (lambda (m) (* 2 (call/pc m (lambda (f)
                                                                                            [d]
                                              (abort m (lambda () f)) )))))
3)
         \rightarrow 6
(splitter
                                                                                           [e1]
 (lambda (m1)
   (* 5 (splitter
        (lambda (m2)
                                                                   ; f2= \lambda u.2 * u
            (* 2 (call/pc m2 (lambda (f2)
```

⁵The presentation of [QS91] is slightly different, we adopt here one of the described variants.

```
(define-class splitter-frame frame ())
(define-class mark Object (q))
(define (ACPS-splitter q f)
  (let* ((frame (make-splitter-frame resume))
         (q (extend q frame)) )
    (f q (make-mark q)) ) )
(define (ACPS-within-extent? q mark)
  (resume q (split q (lambda (q) (eq? q (mark-q mark)))
                   (lambda (frames q) #t)
                   (lambda () #f) )) )
(define (ACPS-abort q mark thunk)
  (split q (lambda (q) (eq? q (mark-q mark)))
         (lambda (frames q) (thunk q))
         (lambda () (error "Out of extent")) ) )
(define (ACPS-call/pc qq mark f)
  (split qq (lambda (q) (eq? q (mark-q mark)))
         (lambda (frames q)
           (f qq (lambda (q v))
                   (resume (extend* q frames) v) )) )
         (lambda () (error "Out of extent")) ) )
```

Figure 5: splitter

(* 3 (call/pc m2 (lambda (f3) ;f3= $\lambda u.(2*(3*u))$ 7))))))))))) \rightarrow 210 *i.e.*, 5*2*3*7 (splitter (lambda (m) [g] (* 5 ((lambda (x) (call/pc m (lambda (f1) (abort m (lambda () x))))) (* 3 (call/pc m (lambda (f2) (abort m (lambda () (* 2 (f2 7))))))))))))) $\rightarrow 21$ ((splitter (lambda (m1) [h] (* 5 (splitter (lambda (m2) (* 2 ((call/pc mi (lambda (f1) ; $f1 = \lambda u . (5 * 2 * (u))(\phi)$ (abort m1 (lambda () (lambda (g) (g f1 m2)))))))))))))))))))) ;; let ϕ be the value of the following term. It will be bound to g. (lambda (f1 m2) (f1 (lambda () (* 7 (call/pc m2 (lambda (f2) (* 11 (f2 13))))))))) \rightarrow Error: out of extent wrt m2

The major differences with spawn are (i) splitter always refers to the lowest associated splitter-frame whereas spawn prefers the nearest one, see example [g]. Partial continuations can in effect duplicate frames which can therefore appear more than once and splitter always refer to the lowest i.e., the one which has been associated to the mark once created. (ii) When applied out of the extent of the corresponding splitter form a partial continuation cannot call again call/pc nor abort as shown in example [h] above.

8.2 Dynamic extent revisited

Dynamic extent is often associated to the lifetime of a computation: dynamic extent ends when the computation returns a value. In presence of high level control operators such as call/cc (and mainly the third effect as mentioned in section 2), determining when a computation ends is difficult (GC can help). At least two views of dynamic extent suggest themselves.

- dynamic extent wrt to a continuation: A computation is within the dynamic extent of a continuation q if the current continuation has q as tail, this is what checks within/de? with eq?.
- dynamic extent wrt to a frame: A computation is within the dynamic extent of a frame if that frame belongs to the current continuation. This is the method **spawn** uses.

The first definition for dynamic extent has the property that when exited, it can be no more entered again. The second allows the dynamic extent to contain "holes", portions of time where the dynamic extent is left.

Example [h] exhibits that difference. With spawn, dynamic extent wrt c2, is captured by f1 and is reinstalled when f1 is called so c2 can be used to reify f2. With splitter, the dynamic extent of m2 is finished as soon as (abort m1 ...) is performed, so trying to reify up to m2 is no longer possible.

Interestingly, dynamic extent requires the implementation of spawn and splitter to use eq? on frames or continuations i.e., needs a store.

8.3 call/cc with splitter/call/pc/abort

Following the tradition, writing call/cc with splitter is possible. This implementation explicitly shows the copy of the interesting stack-slice pc inside the reified continuation. Observe also that call/pc does not remove the reified partial continuation so it is not necessary to call it immediately to reestablish the correct current continuation. Interestingly, the imperative effect performed when invoking continuations is explicit due to the presence of abort in the reified continuation. A definition of splitter in terms of call/cc appears in [QS91].

9 dynamic-wind and call/cc nouveau

The Scheme community has a sort of an equivalent of COMMON LISP's unwind-protect often named dynamic-wind. This form takes three thunks: a prelude, something to do (the real work) and a postlude. The idea is to execute the postlude whenever control escapes from the real work and to execute the prelude whenever control enters again the real work. An operational description can be found in [HF87, FWH92], ACPS allows us to give another one, more functional (without side-effect) and more compact:

Many implementation choices exist in this definition: one can substitute, for instance, (work q2) by (work q1) or, (resume q3 value) by (resume q value) whether one wants to make implementations more efficient or real work less sensitive to the side effects on control that can be performed by pre- or post-ludes. For instance, to write (resume q value) implies that the continuation is always the original caller of the dynamic-wind form whereas (resume q3 value) implies that the continuation of the postlude will be the frames beneath. In general, this is the original caller of the dynamic-wind form unless the frame is copied via partial continuation reification and reinstalled elsewhere.

The dynamic-wind operator only pushes a wind-frame, therefore a new call/cc has to take these frames into account. This new call/cc now creates continuations that, when invoked, unwind the current continuation to execute all postludes until finding a point where the target continuation can be rewound executing all necessary preludes.

Figure 6: dynamic-wind

```
(define (ACPS-new-call/cc qq function)
  (define (rewind q value)
    (define (deepest-wind qq); find the deepest wind-frame in qq till q
      (if (eq? qq q)
          #f
          (or (deepest-wind (cdr qq))
               (if (wind-frame? (car qq)) qq #f) ) ) )
    (let ((wq (deepest-wind qq))) ; evaluate preludes from q to qq
      (if wq ((wind-frame-prelude (car wq))
              (extend (cdr wq)
                       (make-frame
                        (lambda (ignore-q ignore-prelude-value)
                          (rewind wq value) ) )))
          ;; resume the caller of new-call/cc
          (resume qq value) ) ) )
  (define (unwind q value)
    (define (tail? q1 q2) ; is q1 a tail of q2 ?
      (or (eq? q1 q2)
          (and (pair? q2) (tail? q1 (cdr q2))) ) )
    (if (tail? q qq); is q an ancestor of qq
        (rewind q value)
        (if (wind-frame? (car q)) ; evaluate postludes from q
            ((wind-frame-postlude (car q))
             (extend (cdr q)
                      (make-frame
                       (lambda (ignore-q ignore-postlude-value)
                         (unwind (cdr q) value) ) ) )
            (unwind (cdr q) value) ) ) )
  (function qq unwind) )
```

Figure 7: new-call/cc

Many problems are raised by the introduction of dynamic-wind. Not to mention the relationship it carries with partial continuations nor its various possible implementations, it first makes Scheme a purely sequential language with only one possible control point and thus somehow negates the parallel extensions proposed for Scheme. Second, it involves a change in the definition of call/cc that seems to preclude to program the old call/cc with the new one. Third, it makes the formal semantics of Scheme bigger, more complex and, hardly fitting on a single page since the semantics of call/cc grows from a one-liner to half a page.

10 Conclusions

Leaving dynamic-wind apart, the four other sets of control operators can be classified as follows. The first two have a dynamic behavior negated by the last two which allow to specify the point up to which reification is wanted: spawn and splitter make easy to appropriately pair control-like with reset-like operators. reset and spawn incorporate, in the reified partial continuation and as last frame, the frame up to which they were reified. This makes it easy to create a new partial continuation from within a partial continuation invocation. spawn and splitter differ in the amount of reified context as well as in the concept of dynamic extent. It is also unclear what is the "natural" point targeted by a call/pc-like operator if this operator is called from within an applied partial continuation and out of the dynamic extent of the original spawn-like form.

We can now defend two implementation choices: classes and ACPS. Continuations are completely opaque values in Scheme and, besides applying them, it is not possible to inspect them to know if they contain a given frame or continuation tail. We thus had to make this information explicit and therefore could not use a call/cc-based implementation. ACPS, though highly theoretically grounded, is a wonderful tool for that goal and has the additional benefit to be "close" to the implementation i.e., to suggest that continuations are made of frames. Reflection-addicts [dRS, FW84, Wan86, dR87, WF88, DM88] will also appreciate ACPS which allows to represent continuations as list of frames thus opening new opportunities to dissect them.

Classes are useful to factorize the behavior of frames in the **resume** function as well as to allow various control operators to cohabit without interference i.e., without confusing a reset-frame with a wind-frame for instance. Rather than choosing one set of control operators, one may better experiment with all of them simultaneously. In particular, the meaning of dynamic-wind with respect to these control operators is obscure and probably deserve more studies. This also the case of the dynamic extent concept.

We hope that these implementations will allow readers to understand control operators better, try to program with them and appreciate their subtleties.

Acknowledgements

Many thanks for all the readers of the many drafts of this paper and especially among them, Matthias Felleisen and Luc Moreau.

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